## FINAL JEE(Advanced) EXAMINATION - 2022

## (Held On Sunday 28 ${ }^{\text {th }}$ AUGUST, 2022)

## PAPER-1 <br> IEST PAPER WIII SOLUIION

## PHYSICS

## SECTION-1 : (Maximum Marks : 24)

- This section contains EIGHT (08) questions.
- The answer to each question is a NUMERICAL VALUE.
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer. If the numerical value has more than two decimal places, truncate/round-off the value to TWO decimal places.
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks $\quad:+3$ ONLY if the correct numerical value is entered;
Zero Marks : 0 In all other cases.

1. Two spherical stars $A$ and $B$ have densities $\rho_{A}$ and $\rho_{B}$, respectively. $A$ and $B$ have the same radius, and their masses $M_{A}$ and $M_{B}$ are related by $M_{B}=2 M_{A}$. Due to an interaction process, star $A$ loses some of its mass, so that its radius is halved, while its spherical shape is retained, and its density remains $\rho_{A}$. The entire mass lost by $A$ is deposited as a thick spherical shell on $B$ with the density of the shell being $\rho_{A}$. If $\nu_{A}$ and $\nu_{B}$ are the escape velocities from $A$ and $B$ after the interaction process,
the ratio $\frac{v_{B}}{v_{A}}=\sqrt{\frac{10 n}{15^{1 / 3}}}$. The value of $n$ is $\qquad$
Ans. 2.30
Sol. Given $R_{A}=R_{B}=R$
$\mathrm{M}_{\mathrm{B}}=2 \mathrm{M}_{\mathrm{A}}$
Calculation of escape velocity for A:
Radius of remaining star $=\frac{R_{A}}{2}$.
Mass of remaining star $=\rho_{\mathrm{A}} \frac{4}{3} \pi \frac{\mathrm{R}_{\mathrm{A}}^{3}}{8}=\frac{\mathrm{M}_{\mathrm{A}}}{8}$
$\frac{-\mathrm{GM}_{\mathrm{A} / \mathrm{B}}}{\mathrm{R}_{\mathrm{A} / 2}}+\frac{1}{2} \mathrm{mv}_{\mathrm{A}}^{2}=0 \Rightarrow \mathrm{v}_{\mathrm{A}}=\sqrt{\frac{2 \mathrm{GM}_{\mathrm{A} / \mathrm{B}}}{\mathrm{R}_{\mathrm{A} / 2}}}=\sqrt{\frac{\mathrm{GM}_{\mathrm{A}}}{2 \mathrm{R}}}$
Calculation of escape velocity for B
Mass collected over $B=\frac{7}{8} M_{A}$

Let the radius of B becomes r .
$\therefore \frac{4}{3} \pi\left(\mathrm{r}^{3}-\mathrm{R}_{\mathrm{B}}^{3}\right) \rho_{\mathrm{A}}=\frac{7}{8} \rho_{\mathrm{A}} \frac{4}{3} \pi \mathrm{R}_{\mathrm{A}}^{3} \Rightarrow \pi^{3}=\frac{7}{8} \mathrm{R}_{\mathrm{A}}^{3}+\mathrm{R}_{\mathrm{B}}^{3}=\frac{(15)^{1 / 3} \mathrm{R}}{2}$
$\therefore \frac{\mathrm{V}_{\mathrm{B}}^{2}}{2}=\frac{23 \mathrm{GM}_{\mathrm{A}}}{8 \times 15^{1 / 3} \frac{\mathrm{R}}{2}}=\frac{23 \mathrm{GM}_{\mathrm{A}}}{4 \times 15^{1 / 3} \mathrm{R}}$
$\therefore \mathrm{V}_{\mathrm{B}}=\sqrt{\frac{23 \mathrm{GM}_{\mathrm{A}}}{2 \times 15^{1 / 3} \mathrm{R}}}$
$\therefore \frac{\mathrm{V}_{\mathrm{B}}}{\mathrm{V}_{\mathrm{A}}}=\sqrt{\frac{23}{15^{1 / 3}}}=\sqrt{\frac{10 \times 2.30}{15^{1 / 3}}}$
$\mathrm{n}=2.30$
2. The minimum kinetic energy needed by an alpha particle to cause the nuclear reaction ${ }_{7}^{16} \mathrm{~N}+{ }_{2}^{4} \mathrm{He} \rightarrow{ }_{1}^{1} \mathrm{H}+{ }_{8}^{19} \mathrm{O}$ in a laboratory frame is $n$ (in MeV ). Assume that ${ }_{7}^{16} \mathrm{~N}$ is at rest in the laboratory frame. The masses of ${ }_{7}^{16} \mathrm{~N},{ }_{2}^{4} \mathrm{He},{ }_{1}^{1} \mathrm{H}$ and ${ }_{8}^{19} \mathrm{O}$ can be taken to be $16.006 u, 4.003 u$, $1.008 u$ and $19.003 u$, respectively, where $1 u=930 \mathrm{MeVc}^{-2}$. The value of $n$ is $\qquad$ .
Ans. 2.32 to 2.33
Sol. ${ }_{7}^{16} \mathrm{~N}+{ }_{2}^{4} \mathrm{He} \rightarrow{ }_{1}^{1} \mathrm{He}+{ }_{8}^{19} \mathrm{O}$

$$
\begin{aligned}
& { }_{7}^{16} \mathrm{~N}+{ }_{2}^{4} \mathrm{He} \rightarrow \quad{ }_{1}^{1} \mathrm{He}+{ }_{8}^{19} \mathrm{O} \\
& 16.006 \quad 4.003 \quad 1.008 \quad 19.003 \\
& 4 \mathrm{v}_{0}=1 \mathrm{v}_{1}+19 \mathrm{v}_{2}=20 \mathrm{v}_{2} \quad \text { (For max loss of KE) } \\
& \mathrm{v}_{0}=\frac{\mathrm{v}_{2}}{5} \\
&
\end{aligned}
$$

E required $=(1.008+19.003-16.006-4.003) \times 930=1.86$
$\frac{1}{2} 4 \mathrm{v}_{0}^{2}-\frac{1}{2} 20 \mathrm{v}^{2}=1.86$
$\frac{1}{2} 4 \mathrm{v}_{0}^{2}-10 \frac{\mathrm{v}_{0}^{2}}{25} 20 \mathrm{v}^{2}=1.86$
$2 \mathrm{v}_{0}^{2}-\frac{2}{5} \mathrm{v}_{0}^{2}=1.86$
$\frac{8}{5} \mathrm{v}_{0}^{2}=1.86$
$\mathrm{v}_{0}^{2}=\frac{1.86 \times 5}{8}$
$K E=\frac{1}{2} 4 \mathrm{v}_{0}^{2}=2 \mathrm{v}_{0}^{2}=\frac{18.6 \times 5}{4}$
$=2.325$
3. In the following circuit $C_{1}=12 \mu F, C_{2}=C_{3}=4 \mu F$ and $C_{4}=C_{5}=2 \mu F$. The Charge stored in $C_{3}$ is $\qquad$ $\mu C$.


Ans. 8
Sol. Potential difference across the terminals of $\mathrm{C}_{3}$ is 2 V .
$\therefore \mathrm{Q}_{3}=\mathrm{CV}=(4 \mu)(2)=8 \mu \mathrm{C}$
4. A rod of length 2 cm makes an angle $\frac{2 \pi}{3}$ rad with the principal axis of a thin convex lens. The lens has a focal length of 10 cm and is placed at a distance of $\frac{40}{3} \mathrm{~cm}$ from the object as shown in the figure. The height of the image is $\frac{30 \sqrt{3}}{13} \mathrm{~cm}$ and the angle made by it with respect to the principal axis is $\alpha$ rad. The value of $\alpha$ is $\frac{\pi}{n} \mathrm{rad}$, where $n$ is $\qquad$ .


Ans. 6

Sol.


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$\frac{h_{i}}{h_{0}}=\frac{v}{u} \Rightarrow \frac{-\frac{30 \sqrt{3}}{13}}{\sqrt{3}}=\frac{\mathrm{v}}{-\frac{43}{3}} \Rightarrow \mathrm{v}_{1}=\frac{430}{13} \mathrm{~cm}$

* $\frac{1}{\mathrm{v}}-\frac{1}{\mathrm{u}}=\frac{1}{\mathrm{f}} \Rightarrow \frac{1}{\mathrm{v}}=\frac{1}{10}-\frac{3}{40} \Rightarrow \mathrm{v}=40 \mathrm{~cm}$
* $\mathrm{x}=40-\frac{430}{13}=\frac{90}{13} \mathrm{~cm}$
$\tan \alpha=\frac{\frac{30 \sqrt{3}}{13}}{\frac{90}{13}}=\frac{1}{\sqrt{3}} \Rightarrow \alpha=30^{\circ}=\frac{\pi}{6}$
$\mathrm{N}=6$ Ans.

5. At time $t=0$, a disk of radius 1 m starts to roll without slipping on a horizontal plane with an angular acceleration of $\alpha=\frac{2}{3} \mathrm{rad} \mathrm{s}{ }^{-2}$. A small stone is stuck to the disk. At $t=0$, it is at the contact point of the disk and the plane. Later, at time $t=\sqrt{\pi} s$, the stone detaches itself and flies off tangentially from the disk. The maximum height (in $m$ ) reached by the stone measured from the plane is $\frac{1}{2}+\frac{x}{10}$. The value of $x$ is $\qquad$ . [Take $g=10 \mathrm{~m} \mathrm{~s}^{-2}$.]

Ans. 0.52

Sol.


At $t=0, \omega=0$
at $\mathrm{t}=\sqrt{\pi}, \omega=\alpha \mathrm{t}=\frac{2}{3} \sqrt{\pi}, \mathrm{v}=\omega \mathrm{r}=\frac{2}{3} \sqrt{\pi}$
$\theta=\frac{1}{2} \alpha t^{2}$
$\theta=\frac{1}{2} \times \frac{2}{3} \times \pi=\frac{\pi}{3}$
$\theta=60^{\circ}$


$$
v_{y}=v \sin 60=\frac{\sqrt{3}}{2} V
$$

$\mathrm{h}=\frac{\mathrm{u}_{\mathrm{y}}^{2}}{2 \mathrm{~g}}=\frac{\frac{3}{4} \mathrm{v}^{2}}{2 \mathrm{~g}}$
$h=\frac{\frac{3}{4} \times \frac{4}{9} \pi}{2 g}$
$\mathrm{h}=\frac{3 \pi}{9 \times 2 \mathrm{~g}}=\frac{\pi}{6 \mathrm{~g}}$
Maximum height from plane, $H=\frac{R}{2}+h$
$\mathrm{H}=\frac{1}{2}+\frac{\pi}{6 \times 10}$
$\mathrm{x}=\frac{\pi}{6} ; \mathrm{x}=0.52$
6. A solid sphere of mass 1 kg and radius 1 m rolls without slipping on a fixed inclined plane with an angle of inclination $\theta=30^{\circ}$ from the horizontal. Two forces of magnitude $1 N$ each, parallel to the incline, act on the sphere, both at distance $r=0.5 \mathrm{~m}$ from the center of the sphere, as shown in the figure. The acceleration of the sphere down the plane is $\qquad$ $m s^{-2} .\left(\right.$ Take $\left.g=10 m^{-2}.\right)$


Ans. 2.85 to 2.86

Sol. Solid sphere $1 \mathrm{~kg}, 1 \mathrm{~m}$

$5+1-1-\mathrm{f}=1 \mathrm{a}$
$5-\mathrm{f}=\mathrm{a}$
About COM
f $1-2(1(0.5))=\frac{2}{5} \mathrm{Mr}^{2} \alpha$
$\Rightarrow \mathrm{f}-1=\frac{2}{5} \mathrm{a} \Rightarrow \mathrm{f}=1+\frac{2}{5} \mathrm{a}$
$5-\mathrm{a}=1+\frac{2}{5} \mathrm{a}$
$\Rightarrow 4=\frac{7 \mathrm{a}}{5} \Rightarrow \mathrm{a}=\frac{20}{7}=2.86 \mathrm{~m} / \mathrm{s}^{2}$
7. Consider an LC circuit, with inductance $\mathrm{L}=0.1 \mathrm{H}$ and capacitance $C=10^{-3} \mathrm{~F}$, kept on a plane. The area of the circuit is $1 \mathrm{~m}^{2}$. It is placed in a constant magnetic field of strength $B_{0}$ which is perpendicular to the plane of the circuit. At time $t=0$, the magnetic field strength starts increasing linearly as $B=B_{0}+\beta \mathrm{t}$ with $\beta=0.04 \mathrm{Ts}^{-1}$. The maximum magnitude of the current in the circuit is $\qquad$ $m A$.
Ans. 4
Sol. Maximum energy will be
$\frac{\mathrm{q}_{0}^{2}}{2 \mathrm{C}}=\frac{1}{2} \mathrm{LI}_{0}^{2}$
$\frac{\mathrm{q}_{0}^{2}}{\mathrm{CL}}=\mathrm{I}_{0}^{2}$
$\mathrm{I}_{0}=\frac{\mathrm{q}_{0}}{\sqrt{\mathrm{LC}}}$
$\mathrm{I}_{0}=\frac{\mathrm{CV}}{\sqrt{\mathrm{LC}}}$
$\mathrm{I}_{0}=\sqrt{\frac{\mathrm{C}}{\mathrm{L}}} \times \mathrm{V} \quad \mathrm{V}=\mathrm{emf}=\left|\frac{\mathrm{AdB}}{\mathrm{dt}}\right|$
$I_{0}=\sqrt{\frac{10^{-3}}{0.1}} \times 0.04 \quad V=(1 \times 0.04)$
Maximum current $\mathrm{I}_{0}=0.004=4 \mathrm{~mA}$
Ans. (4)
8. A projectile is fired from horizontal ground with speed $v$ and projection angle $\theta$. When the acceleration due to gravity is $g$, the range of the projectile is $d$. If at the highest point in its trajectory, the projectile enters a different region where the effective acceleration due to gravity is $g^{\prime}=\frac{g}{0.81}$, then the new range is $d^{\prime}=n d$. The value of $n$ is $\qquad$ .

Ans. 0.95

Sol.

$\mathrm{d}=\frac{\mathrm{v}^{2} \sin 2 \theta}{\mathrm{~g}}$

$\mathrm{H}_{\text {max }}=\frac{\mathrm{v}^{2} \sin ^{2} \theta}{2 \mathrm{~g}} ; \frac{1}{2} \mathrm{~g}_{\text {eff }} \mathrm{t}^{2}=\mathrm{H}_{\text {max }} \Rightarrow \mathrm{t}^{2}=\frac{2 \mathrm{H}_{\text {max }}}{\mathrm{g}_{\text {eff }}} ; \mathrm{t}=\sqrt{\frac{\mathrm{v}^{2} \sin ^{2} \theta \times 0.81}{\mathrm{~g}^{2}}} ; \mathrm{t}=\frac{0.9 \mathrm{v} \sin \theta}{\mathrm{g}}$
$\mathrm{t}^{2}=\frac{2 \times \mathrm{v}^{2} \sin ^{2} \theta}{2 \mathrm{~g}\left(\frac{\mathrm{~g}}{0.81}\right)}$
$d^{\prime}=$ New range $=\frac{d}{2}+d_{1}$
$\mathrm{d}_{1}=\mathrm{vcos} \theta^{\circ} \mathrm{t}$
$=\frac{\mathrm{v}^{2} \sin ^{2} \theta \cos \theta \times 0.9}{\mathrm{~g}} ; \mathrm{d}^{\prime}=\frac{\mathrm{v}^{2} \sin 2 \theta}{2 \mathrm{~g}}+\frac{\mathrm{v}^{2} \sin 2 \theta \times 0.9}{2 \mathrm{~g}}$
$=\frac{\mathrm{v}^{2} \sin 2 \theta}{\mathrm{~g}}\left(\frac{1.0}{2}\right)=0.95 \mathrm{~d}$
$\mathrm{n}=0.95$

## SECTION-2 : (Maximum Marks : 24)

- This section contains SIX (06) questions.
- Each question has FOUR options (A), (B), (C) and (D). ONE OR MORE THAN ONE of these four option(s) is (are) correct answer(s).
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated according to the following marking scheme:

Full Marks $\quad:+4$ ONLY if (all) the correct option(s) is(are) chosen;
Partial Marks : $: 3$ If all the four options are correct but ONLY three options are chosen;
Partial Marks $\quad:+2$ If three or more options are correct but ONLY two options are chosen, both of which are correct;
Partial Marks : +1 If two or more options are correct but ONLY one option is chosen and it is a correct option;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered); Negative Marks :-2 In all other cases.
9. A medium having dielectric constant $K>1$ fills the space between the plates of a parallel plate capacitor. The plates have large area, and the distance between them is $d$. The capacitor is connected to a battery of voltage $V$. as shown in Figure (a). Now, both the plates are moved by a distance of $\frac{d}{2}$ from their original positions, as shown in Figure (b).


Figure (a)


Figure (b)

In the process of going from the configuration depicted in Figure (a) to that in Figure (b), which of the following statement(s) is(are) correct?
(A) The electric field inside the dielectric material is reduced by a factor of $2 K$.
(B) The capacitance is decreased by a factor of $\frac{1}{K+1}$.
(C) The voltage between the capacitor plates is increased by a factor of $(K+1)$.
(D) The work done in the process DOES NOT depend on the presence of the dielectric material.

Ans. (B)

Sol. For figure(a)


$$
\mathrm{E}_{0}=\frac{\mathrm{V}}{\mathrm{~d}} ; \mathrm{C}=\frac{\mathrm{K} \varepsilon_{0} \mathrm{~A}}{\mathrm{~d}}
$$

For figure(b)

$\mathrm{C}^{\prime}=\frac{\varepsilon_{0} \mathrm{~A}}{2 \mathrm{~d}-\mathrm{d}+\mathrm{d} / \mathrm{k}} ;$
$\mathrm{C}^{\prime}=\frac{\mathrm{K} \varepsilon_{0} \mathrm{~A}}{(\mathrm{~K}+1) \mathrm{d}} ; \mathrm{C}^{\prime}=\frac{\mathrm{C}}{\mathrm{K}+1}$
10. The figure shows a circuit having eight resistances of $1 \Omega$ each, labelled $R_{1}$ to $R_{8}$, and two ideal batteries with voltages $\varepsilon_{1}=12 \mathrm{~V}$ and $\varepsilon_{2}=6 \mathrm{~V}$.


Which of the following statement(s) is(are) correct?
(A) The magnitude of current flowing through $R_{1}$ is $7.2 A$.
(B) The magnitude of current flowing through $R_{2}$ is 1.2 A .
(C) The magnitude of current flowing through $R_{3}$ is 4.8 A .
(D) The magnitude of current flowing through $R_{5}$ is 2.4 A .

Ans. (A,B,C,D)

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Sol.



From KCL
$\mathrm{i}_{1}+\mathrm{i}_{2}+\mathrm{i}_{3}=0$
$\Rightarrow \frac{18-\mathrm{V}_{0}}{3 / 2}+\frac{12-\mathrm{V}_{0}}{1 / 2}+\frac{0-\mathrm{V}_{0}}{3 / 2}=0$
$\Rightarrow 18-\mathrm{V}_{0}+36-3 \mathrm{~V}_{0}-\mathrm{V}_{0}=0$
$\Rightarrow 54=5 \mathrm{~V}_{0}$
$\frac{2\left(\frac{54}{5}-v^{\prime}\right)}{1}+\frac{18-v^{\prime}}{1}=0$
$\Rightarrow \frac{108}{5}+18=3 \mathrm{~V}^{\prime}$
$\Rightarrow \mathrm{v}^{\prime}=\frac{198}{5 \times 3}=\frac{66}{5} \mathrm{~V}$
$I_{R_{1}}=\frac{36}{5}=7.2 \mathrm{~A}$
$\mathrm{I}_{\mathrm{R}_{2}}=\frac{6}{5}=1.2 \mathrm{~A}$
$\mathrm{I}_{\mathrm{R}_{3}}=\frac{24}{5}=4.8 \mathrm{~A}$
$\mathrm{I}_{\mathrm{R}_{5}}=\frac{12}{5}=2.4 \mathrm{~A}$
11. An ideal gas of density $\rho=0.2 \mathrm{~kg} \mathrm{~m}^{-3}$ enters a chimney of height h at the rate of $\alpha=0.8 \mathrm{~kg} \mathrm{~s}{ }^{-1}$ from its lower end, and escapes through the upper end as shown in the figure. The cross-sectional area of the lower end is $A_{1}=0.1 \mathrm{~m}^{2}$ and the upper end is $A_{2}=0.4 \mathrm{~m}^{2}$. The pressure and the temperature of the gas at the lower end are 600 Pa and 300 K , respectively, while its temperature at the upper end is 150 K . The chimney is heat insulated so that the gas undergoes adiabatic expansion. Take $g=10 \mathrm{~ms}^{-2}$ and the ratio of specific heats of the gas $\gamma=2$. Ignore atmospheric pressure.


Which of the following statement(s) is(are) correct?
(A) The pressure of the gas at the upper end of the chimney is 300 Pa .
(B) The velocity of the gas at the lower end of the chimney is $40 \mathrm{~ms}^{-1}$ and at the upper end is $20 \mathrm{~ms}^{-1}$.
(C) The height of the chimney is 590 m .
(D) The density of the gas at the upper end is $0.05 \mathrm{~kg} \mathrm{~m}^{-3}$.

Ans. (B)
Sol.

$\frac{\mathrm{dm}}{\mathrm{dt}}=\rho_{1} \mathrm{~A}_{1} \mathrm{v}_{1}=0.8 \mathrm{~kg} / \mathrm{s} \mathrm{A}$
$\mathrm{v}_{1}=\frac{0.8}{0.2 \times 0.1}=40 \mathrm{~m} / \mathrm{s}$
$\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$
$\gamma=2$
Gas undergoes adiabatic expansion,
$\mathrm{p}^{1-\gamma} \mathrm{T}^{\gamma}=$ Constant
$\frac{\mathrm{P}_{2}}{\mathrm{P}_{1}}=\left(\frac{\mathrm{T}_{1}}{\mathrm{~T}_{2}}\right)^{\frac{\mathrm{r}}{1-\gamma}}$
$P_{2}=\left(\frac{300}{150}\right)^{\frac{2}{-1}} \times 600$
$P_{2}=\frac{600}{4}=150 \mathrm{~Pa}$
Now $\rho=\frac{\mathrm{PM}}{\mathrm{RT}} \Rightarrow \rho \propto \frac{\mathrm{P}}{\mathrm{T}}$
$\frac{\rho_{1}}{\rho_{2}}=\left(\frac{\mathrm{P}_{1}}{\mathrm{P}_{2}}\right)\left(\frac{\mathrm{T}_{1}}{\mathrm{~T}_{2}}\right)=\left(\frac{150}{600}\right)\left(\frac{300}{150}\right)=\frac{1}{2}$
$\rho_{2}=\frac{\rho_{1}}{2}=0.1 \mathrm{~kg} / \mathrm{m}^{3}$
Now $\rho_{2} \mathrm{~A}_{2} \mathrm{v}_{2}=0.8 \Rightarrow \mathrm{v}_{2}=\frac{0.8}{0.1 \times 0.4}=20 \mathrm{~m} / \mathrm{s}$
Now $\mathrm{W}_{\text {on gas }}=\Delta \mathrm{K}+\Delta \mathrm{U}+$ (Internal energy)
$\mathrm{P}_{1} \mathrm{~A}_{1} \Delta \mathrm{x}_{1}-\mathrm{P}_{2} \mathrm{~A}_{2} \Delta \mathrm{x}_{2}=\frac{1}{2} \Delta \mathrm{mV}_{2}^{2}-\frac{1}{2} \Delta \mathrm{mV} \mathrm{V}_{1}^{2}+\Delta \mathrm{mgh}+\frac{\mathrm{f}}{2}\left(\mathrm{P}_{2} \Delta \mathrm{~V}_{2}-\mathrm{P}_{1} \Delta \mathrm{~V}_{1}\right)$
$\Rightarrow 2 \mathrm{P}_{1} \frac{\Delta \mathrm{~V}_{1}}{\Delta \mathrm{~m}}-2 \mathrm{P}_{2} \frac{\Delta \mathrm{~V}_{2}}{\Delta \mathrm{~m}}=\frac{\mathrm{V}_{2}^{2}-\mathrm{V}_{1}^{2}}{2}+\mathrm{gh}$
$\Rightarrow \frac{2 \times 600}{0.2}-\frac{2 \times 150}{0.1}=\frac{20^{2}-40^{2}}{2}+10 \mathrm{~h}$
$\mathrm{h}=360 \mathrm{~m}$

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12. Three plane mirrors form an equilateral triangle with each side of length $L$. There is a small hole at a distance $l>0$ from one of the corners as shown in the figure. A ray of light is passed through the hole at an angle $\theta$ and can only come out through the same hole. The cross section of the mirror configuration and the ray of light lie on the same plane.


Which of the following statement(s) is(are) correct?
(A) The ray of light will come out for $\theta=30^{\circ}$, for $0<l<L$.
(B) There is an angle for $l=\frac{L}{2}$ at which the ray of light will come out after two reflections.
(C) The ray of light will NEVER come out for $\theta=60^{\circ}$, and $l=\frac{L}{3}$.
(D) The ray of light will come out for $\theta=60^{\circ}$, and $0<l<\frac{L}{2}$ after six reflections.

Ans. (A,B)
Sol. (A) Ray will come out after one reflection for $\theta=30^{\circ} \& 0<\ell<\mathrm{L}$

(B)

for $\theta=60^{\circ} \& \ell=\frac{L}{2}$, ray will come out after two reflections.
(C) For $\ell=\frac{\mathrm{L}}{3} \& \theta=60^{\circ}$ ray will come out after five reflections.

(D) $\operatorname{For} \theta=60^{\circ} \& 0<\ell<\frac{\mathrm{L}}{2}$, ray will come out after five reflections

13. Six charges are placed around a regular hexagon of side length a as shown in the figure. Five of them have charge $q$, and the remaining one has charge $x$. The perpendicular from each charge to the nearest hexagon side passes through the center O of the hexagon and is bisected by the side.


Which of the following statement(s) is(are) correct in SI units?
(A) When $x=q$, the magnitude of the electric field at O is zero.
(B) When $x=-q$, the magnitude of the electric field at O is $\frac{q}{6 \pi \in_{0} a^{2}}$.
(C) When $x=2 q$, the potential at O is $\frac{7 q}{4 \sqrt{3} \pi \epsilon_{0} a}$.
(D) When $x=-3 q$, the potential at O is $\frac{3 q}{4 \sqrt{3} \pi \in_{0} a}$.

Ans. (A,B,C)
Sol. (A) Due to symmetry $\overrightarrow{\mathrm{E}}_{0}=0$

$\mathrm{E}_{\text {net }}=\frac{\mathrm{kq}}{(2 \mathrm{~d})^{2}} \times 2=\frac{2 \mathrm{q} \times 4}{4 \pi \varepsilon_{0} \cdot 4 \cdot 3 \mathrm{a}^{2}}$
$=\frac{\mathrm{q}}{6 \pi \varepsilon_{0} \mathrm{a}^{2}}$
(C) $\mathrm{v}=\frac{7 \mathrm{kq}}{2 \mathrm{~d}}=\frac{7 \mathrm{q}}{4 \pi \varepsilon_{0} \cdot \sqrt{3} \mathrm{a}}=\frac{7 \mathrm{q}}{4 \sqrt{3} \pi \varepsilon_{0} \mathrm{q}}$
(D) $\mathrm{v}=\frac{2 \mathrm{kq}}{2 \mathrm{~d}}=\frac{2 \mathrm{q}}{4 \pi \varepsilon_{0} \cdot \sqrt{3} \mathrm{a}}=\frac{\mathrm{q}}{2 \sqrt{3} \pi \varepsilon_{0} \mathrm{q}}$

Ans. (A,B,C)
14. The binding energy of nucleons in a nucleus can be affected by the pairwise Coulomb repulsion. Assume that all nucleons are uniformly distributed inside the nucleus. Let the binding energy of a proton be $E_{b}^{p}$ and the binding energy of a neutron be $E_{b}^{n}$ in the nucleus.

Which of the following statement(s) is(are) correct?
(A) $E_{b}^{p}-E_{b}^{n}$ is proportional to $Z(Z-1)$ where $Z$ is the atomic number of the nucleus.
(B) $E_{b}^{p}-E_{b}^{n}$ is proportional to $A^{-\frac{1}{3}}$ where $A$ is the mass number of the nucleus.
(C) $E_{b}^{p}-E_{b}^{n}$ is positive.
(D) $E_{b}^{p}$ increases if the nucleus undergoes a beta decay emitting a positron.

## Ans. (A,B,D)

Sol. Binding energy of proton $\&$ neutron due to nuclear force is same. So difference in binding energy is only due to electrostatic P.E. and it is positive
$\mathrm{E}_{0}^{\mathrm{p}}-\mathrm{E}_{0}^{\mathrm{n}}=$ electrostatic P.E.
$=\mathrm{Z} \times$ P.E. of one proton
$=\mathrm{Z} \times \frac{1}{4 \pi \varepsilon_{0}} \frac{(\mathrm{Z}-1) \mathrm{e}^{2}}{\mathrm{R}}$
Where $R=R_{0} A^{1 / 3}$
$=\frac{1}{4 \pi \varepsilon_{0}} \frac{\mathrm{Z}(\mathrm{Z}-1) \mathrm{e}^{2}}{\mathrm{R}_{0} \mathrm{~A}^{\frac{1}{3}}}$

## Ans. (A,B,D)

## SECTION-3 : (Maximum Marks : 12)

- This section contains FOUR (04) Matching List Sets.
- Each set has ONE Multiple Choice Question.
- Each set has TWO lists : List-I and List-II.
- List-I has Four entries (I), (II), (III) and (IV) and List-II has Five entries (P), (Q), (R), (S) and (T).
- FOUR options are given in each Multiple Choice Question based on List-I and List-II and ONLY

ONE of these four options satisfies the condition asked in the Multiple Choice Question.

- Answer to each question will be evaluated according to the following marking scheme:

Full Marks $\quad:+3$ ONLY if the option corresponding to the correct combination is chosen;
Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);
Negative Marks : -1 In all other cases.
15. A small circular loop of area $A$ and resistance $R$ is fixed on a horizontal $x y$-plane with the center of the loop always on the axis $\hat{n}$ of a long solenoid. The solenoid has $m$ turns per unit length and carries current $I$ counterclockwise as shown in the figure. The magnetic field due to the solenoid is in $\hat{\mathrm{n}}$ direction. List-I gives time dependences of $\hat{\mathrm{n}}$ in terms of a constant angular frequency $\omega$. List-II gives the torques experienced by the circular loop at time $t=\frac{\pi}{6 \omega}$, Let $\alpha=\frac{A^{2} \mu_{0}^{2} m^{2} I^{2} \omega}{2 R}$.


| List-I |  | List-II |  |
| :--- | :--- | :--- | :--- |
| (I) | $\frac{1}{\sqrt{2}}(\sin \omega t \hat{j}+\cos \omega t \hat{k})$ | (P) | 0 |
| (II) | $\frac{1}{\sqrt{2}}(\sin \omega t \hat{i}+\cos \omega t \hat{j})$ | (Q) | $-\frac{\alpha}{4} \hat{i}$ |
| (III) | $\frac{1}{\sqrt{2}}(\sin \omega t \hat{i}+\cos \omega t \hat{k})$ | (R) | $\frac{3 \alpha}{4} \hat{i}$ |
| (IV) | $\frac{1}{\sqrt{2}}(\cos \omega t \hat{i}+\sin \omega t \hat{k})$ | (S) | $\frac{\alpha}{4} \hat{j}$ |
|  |  | (T) | $-\frac{3 \alpha}{4} \hat{i}$ |

Which one of the following options is correct?
(A) I $\rightarrow \mathrm{Q}, \mathrm{II} \rightarrow \mathrm{P}, \mathrm{III} \rightarrow \mathrm{S}, \mathrm{IV} \rightarrow \mathrm{T}$
(B) $\mathrm{I} \rightarrow \mathrm{S}, \mathrm{II} \rightarrow \mathrm{T}, \mathrm{III} \rightarrow \mathrm{Q}, \mathrm{IV} \rightarrow \mathrm{P}$
(C) I $\rightarrow \mathrm{Q}, \mathrm{II} \rightarrow \mathrm{P}, \mathrm{III} \rightarrow \mathrm{S}, \mathrm{IV} \rightarrow \mathrm{R}$
(D) I $\rightarrow \mathrm{T}, \mathrm{II} \rightarrow \mathrm{Q}, \mathrm{III} \rightarrow \mathrm{P}, \mathrm{IV} \rightarrow \mathrm{R}$

Ans. (C)

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Sol. (I) $\overrightarrow{\mathrm{B}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}}(\sin \omega t \hat{\mathrm{j}}+\cos \omega \mathrm{t} \hat{\mathrm{k}})$

$$
\begin{aligned}
& \phi=\overrightarrow{\mathrm{B}} \cdot \overrightarrow{\mathrm{~A}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}} \cos (\omega \mathrm{t}) \cdot \mathrm{A} \\
& \varepsilon=\frac{\mathrm{d} \phi}{\mathrm{dt}}=\frac{\mu_{0} \mathrm{mI} \omega \mathrm{~A}}{\sqrt{2}} \sin (\omega \mathrm{t}) \\
& \mathrm{i}=\frac{\varepsilon}{\mathrm{R}}=\frac{\mu_{0} \mathrm{mI} \omega \mathrm{~A}}{\sqrt{2} \mathrm{R}} \sin (\omega \mathrm{t}) \\
& \overrightarrow{\mathrm{M}}=\mathrm{i} \overrightarrow{\mathrm{~A}}=\mathrm{iA}(\hat{\mathrm{k}})=\frac{\mu_{0} \mathrm{mI}^{2} \omega \mathrm{~A}^{2}}{\sqrt{2} \mathrm{R}} \sin (\omega \mathrm{t})(\hat{\mathrm{k}}) \\
& \vec{\tau}=\overrightarrow{\mathrm{M}} \times \overrightarrow{\mathrm{B}}=\frac{\mu_{0} \mathrm{~m}^{2} \mathrm{I}^{2} \omega \mathrm{~A}^{2}}{\sqrt{2} \mathrm{R}} \sin ^{2}(\omega \mathrm{t})(-\hat{\mathrm{i}}) \\
& =-\left(\frac{\alpha}{4}\right) \hat{\mathrm{i}}
\end{aligned}
$$

(II) $\overrightarrow{\mathrm{B}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}}(\sin \omega t \hat{\mathrm{i}}+\cos \omega \mathrm{t} \hat{\mathrm{j}})$
$\phi=0, \varepsilon=0, \mathrm{i}=0, \mathrm{t}=0$
(III) $\overrightarrow{\mathrm{B}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}}(\sin \omega \mathrm{t} \hat{\mathrm{i}}+\cos \omega \mathrm{t} \hat{\mathrm{k}})$

$$
\phi=\overrightarrow{\mathrm{B}} \cdot \overrightarrow{\mathrm{~A}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}} \cdot \cos (\omega \mathrm{t}) \cdot \mathrm{A}
$$

$$
\varepsilon=-\frac{\mathrm{d} \phi}{\mathrm{dt}}=\frac{\mu_{0} \mathrm{mI} \omega \mathrm{~A}}{\sqrt{2}} \sin (\omega \mathrm{t})
$$

## éSaral

$\mathrm{i}=\frac{\varepsilon}{\mathrm{R}}=\frac{\mu_{0} \mathrm{mI} \omega \mathrm{A}}{\sqrt{2} \mathrm{R}} \sin (\omega \mathrm{t})$
$\vec{M}=i \vec{A}=i A(\hat{k})=\frac{\mu_{0} m I \omega A^{2}}{\sqrt{2} R} \sin (\omega t)(\hat{k})$
$\vec{\tau}=\overrightarrow{\mathrm{M}} \times \overrightarrow{\mathrm{B}}=\frac{\mu_{0} \mathrm{~m}^{2} \mathrm{I}^{2} \omega \mathrm{~A}^{2}}{2 \mathrm{R}} \sin ^{2}(\omega \mathrm{t})(+\hat{\mathrm{j}})$
$=\frac{\alpha}{4} \hat{j}$
(IV) $\overrightarrow{\mathrm{B}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}}(\cos \omega t \hat{\mathrm{j}}+\sin \omega t \hat{\mathrm{k}})$
$\phi=\overrightarrow{\mathrm{B}} \cdot \overrightarrow{\mathrm{A}}=\frac{\mu_{0} \mathrm{mI}}{\sqrt{2}} \cdot \sin (\omega \mathrm{t}) \cdot \mathrm{A}$
$\varepsilon=-\frac{\mathrm{d} \phi}{\mathrm{dt}}=\frac{\mu_{0} \mathrm{mI} \omega \mathrm{A}}{\sqrt{2}} \cos (\omega \mathrm{t})$
$\mathrm{i}=\frac{\varepsilon}{\mathrm{R}}=-\frac{\mu_{0} \mathrm{mI} \omega \mathrm{A}}{\sqrt{2} \mathrm{R}} \cos (\omega \mathrm{t})$
$\vec{M}=i \vec{A}=i A(\hat{k})=-\frac{\mu_{0} m I \omega A^{2}}{\sqrt{2} R} \cos (\omega t)(\hat{k})$
$\vec{\tau}=\overrightarrow{\mathrm{M}} \times \overrightarrow{\mathrm{B}}=-\frac{\mu_{0} \mathrm{~m}^{2} \mathrm{I}^{2} \omega \mathrm{~A}^{2}}{2 \mathrm{R}} \cos ^{2}(\omega \mathrm{t})(-\hat{\mathrm{i}})$
$=\alpha \cdot \cos ^{2}\left(\frac{\pi}{6}\right) \hat{\mathrm{i}}$
$=\frac{3 \alpha}{4} \hat{i}$

Ans. (C) I-Q, II-P, III-S, IV-R
16. List I describes four systems, each with two particles $A$ and $B$ in relative motion as shown in figure.

List II gives possible magnitudes of then relative velocities (in $m s^{-1}$ ) at time $t=\frac{\pi}{3} s$.

| List-I |  | List-II |  |
| :---: | :---: | :---: | :---: |
| (I) | $A$ and $B$ are moving on a horizontal circle of radius $1 m$ with uniform angular speed $\omega=1 \mathrm{rad} \mathrm{s}^{-1}$. The initial angular positions of $A$ and $B$ at time $t=0$ are $\theta=0$ and $\theta=\frac{\pi}{2}$ respectively. | (P) | $\frac{\sqrt{3}+1}{2}$ |
| (II) | Projectiles $A$ and $B$ are fired (in the same vertical plane) at $t=0$ and $t=0.1 \mathrm{~s}$ respectively, with the same speed $v=\frac{5 \pi}{\sqrt{2}} \mathrm{~m} \mathrm{~s}^{-1}$ and at $45^{\circ}$ from the horizontal plane. The initial separation between $A$ and $B$ is large enough so that they do not collide, $\left(g=10 \mathrm{~m} \mathrm{~s}^{-2}\right)$. | (Q) | $\frac{(\sqrt{3}-1)}{\sqrt{2}}$ |
| (III) | Two harmonic oscillators $A$ and $B$ moving in the $x$ direction according to $x_{A}=x_{0} \quad \sin \frac{t}{t_{0}}$ and $x_{B}=x_{0} \sin \left(\frac{t}{t_{0}}+\frac{\pi}{2}\right)$ respectively, starting from $t=0$. Take $x_{0}=1 \mathrm{~m}, t_{0}=1 \mathrm{~s}$. | (R) | $\sqrt{10}$ |

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| (IV) | Particle $A$ is rotating in a horizontal circular path of radius <br> $1 m$ on the $x y$ plane, with constant angular speed $\omega=1 \mathrm{rads}^{-1}$. <br> Particle $B$ is moving up at a constant speed $3 \mathrm{~ms}^{-1}$ in the <br> vertical direction as shown in the figure. (Ignore gravity.) | (S) | $\sqrt{2}$ |
| :--- | :--- | :--- | :--- |
|  |  |  |  |

Which one of the following options is correct?
(A) I $\rightarrow$ R, II $\rightarrow$ T, III $\rightarrow \mathrm{P}, \mathrm{IV} \rightarrow \mathrm{S}$
(B) I $\rightarrow \mathrm{S}, \mathrm{II} \rightarrow \mathrm{P}, \mathrm{III} \rightarrow \mathrm{Q}, \mathrm{IV} \rightarrow \mathrm{R}$
(C) I $\rightarrow$ S, II $\rightarrow$ T, III $\rightarrow$ P, IV $\rightarrow R$
(D) I $\rightarrow$ T, II $\rightarrow$ P, III $\rightarrow$ R, IV $\rightarrow$ S

Ans. (C)
Sol. (I) $\mathrm{v}_{\mathrm{BA}}^{2}=\mathrm{v}_{\mathrm{A}}^{2}+\mathrm{v}_{\mathrm{B}}^{2}-2 \mathrm{v}_{\mathrm{AB}} \cos \theta$

As $\omega_{\mathrm{A}}=\omega_{\mathrm{B}}, \theta=90^{\circ}$ remains constant.

Also, $\mathrm{v}_{\mathrm{A}}=\mathrm{v}_{\mathrm{B}}=1 \mathrm{~m} / \mathrm{s}$
So, $\mathrm{v}_{\mathrm{BA}}=\sqrt{2} \mathrm{~m} / \mathrm{s}$
(II) $\overrightarrow{\mathrm{u}}_{\mathrm{A}}=\frac{5 \pi}{2} \hat{\mathrm{i}}+\frac{5 \pi}{2} \hat{\mathrm{j}}$
$\overrightarrow{\mathrm{v}}_{\mathrm{A}}=\frac{5 \pi}{2} \hat{\mathrm{i}}+\left(\frac{5 \pi}{2}-10 \cdot \frac{\pi}{3}\right) \hat{\mathrm{j}}$
$=\frac{5 \pi}{2} \hat{\mathrm{i}}-\frac{5 \pi}{6} \hat{\mathrm{j}}$
$\overrightarrow{\mathrm{u}}_{\mathrm{B}}=-\frac{5 \pi}{2} \hat{\mathrm{i}}+\frac{5 \pi}{2} \hat{\mathrm{j}}$
$\overrightarrow{\mathrm{u}}_{\mathrm{B}}=-\frac{5 \pi}{2} \hat{\mathrm{i}}-\left(\frac{5 \pi}{6}+1\right) \hat{\mathrm{j}}$
$\overrightarrow{\mathrm{v}}_{\mathrm{B}, \mathrm{A}}=-5 \pi \hat{\mathrm{i}}-\hat{\mathrm{j}}$
$\mathrm{v}_{\mathrm{BA}}=\sqrt{25 \pi^{2}+1}$
(III) $\mathrm{x}_{\mathrm{A}}=\sin \mathrm{t}$
$\mathrm{v}_{\mathrm{A}}=\cos \mathrm{t}=\frac{1}{2} \mathrm{~m} / \mathrm{s}$
$\mathrm{x}_{\mathrm{B}}=\operatorname{cost}$
$v_{B}=-\sin t=-\frac{\sqrt{3}}{2} \mathrm{~m} / \mathrm{s}$
$\mathrm{V}_{\mathrm{BA}}=-\frac{\sqrt{3}}{2}-\frac{1}{2}$
(IV) $\overrightarrow{\mathrm{v}}_{\mathrm{A}} \& \overrightarrow{\mathrm{v}}_{\mathrm{B}}$ are always perpendicular

So, $\left|\overrightarrow{\mathrm{v}}_{\mathrm{BA}}\right|=\sqrt{\mathrm{v}_{\mathrm{A}}^{2}+\mathrm{v}_{\mathrm{B}}^{2}}=\sqrt{10} \mathrm{~m} / \mathrm{s}$
Ans. (C), I-S, II-T, III-P, IV-R
17. List I describes thermodynamic processes in four different systems. List II gives the magnitudes (either exactly or as a close approximation) of possible changes in the internal energy of the system due to the process.

| List-I |  | List-II |  |
| :---: | :---: | :---: | :---: |
| (I) | $10^{-3} \mathrm{~kg}$ of water at $100^{\circ} \mathrm{C}$ is converted to steam at the same temperature, at a pressure of $10^{5} \mathrm{~Pa}$. The volume of the system changes from $10^{-6} \mathrm{~m}^{3}$ to $10^{-3} \mathrm{~m}^{3}$ in the process. Latent heat of water $=2250 \mathrm{~kJ} / \mathrm{kg}$. | (P) | 2 kJ |
| (II) | 0.2 moles of a rigid diatomic ideal gas with volume $V$ at temperature 500 K undergoes an isobaric expansion to volume 3 V . Assume $R=8.0 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$. | (Q) | 7 kJ |
| (III) | On mole of a monatomic ideal gas is compressed adiabatically from volume $V=\frac{1}{3} m^{3}$ and pressure 2 kPa to volume $\frac{v}{8}$ | (R) | 4 kJ |
| (IV) | Three moles of a diatomic ideal gas whose molecules can vibrate, is given 9 kJ of heat and undergoes isobaric expansion. | (S) | 5 kJ |
|  |  | (T) | 3 kJ |

Which one of the following options is correct?
(A) I $\rightarrow$ T, II $\rightarrow$ R, III $\rightarrow$ S, IV $\rightarrow$ Q
(B) I $\rightarrow$ S, II $\rightarrow$ P, III $\rightarrow$ T, IV $\rightarrow \mathrm{P}$
(C) I $\rightarrow$ P, II $\rightarrow$ R, III $\rightarrow$ T, IV $\rightarrow$ Q
(D) I $\rightarrow$ Q, II $\rightarrow$ R, III $\rightarrow$ S, IV $\rightarrow \mathrm{T}$

Ans. (C)

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Sol. (I) $\Delta U=\Delta Q-\Delta W$
$=\left\{\left(10^{-3} \times 2250\right)-\frac{10^{5}\left(10^{-3}-10^{-6}\right)}{10^{3}}\right\} \mathrm{kJ}$
$=(2.25-0.0999) \mathrm{kJ}$
$=(2.1501) \mathrm{kJ}$
(II) $\Delta \mathrm{U}=\mathrm{nC}_{\mathrm{V}} \Delta \mathrm{T}$

$$
\begin{aligned}
& =\frac{5}{2} \mathrm{nR} \Delta \mathrm{~T} \\
& =\frac{5}{2} \cdot(0.2)(8)(1500-500) \mathrm{J} \\
& =4 \mathrm{~kJ}
\end{aligned}
$$

(III) $\mathrm{P}_{1} \mathrm{~V}_{2}^{\gamma}=\mathrm{P}_{2} \mathrm{~V}_{2}^{\gamma}$

$$
\begin{aligned}
& \Rightarrow 2\left(\frac{1}{3}\right)^{5 / 3}=\mathrm{P}_{2}\left(\frac{1}{24}\right)^{5 / 3} \\
& \Rightarrow \mathrm{P}_{2}=64 \mathrm{kPa} \\
& \Delta \mathrm{U}=\mathrm{nC}_{\mathrm{v}} \Delta \mathrm{~T}=\frac{3}{2} \cdot\left(\mathrm{P}_{2} \mathrm{~V}_{2}-\mathrm{P}_{1} \mathrm{~V}_{1}\right) \\
& =\frac{3}{2}\left(64 \times \frac{1}{24}-2 \times \frac{1}{3}\right) \mathrm{kJ} \\
& =3 \mathrm{~kJ}
\end{aligned}
$$

(IV) $\Delta \mathrm{U}=\mathrm{nC}_{\mathrm{v}} \Delta \mathrm{T}$

$$
\begin{aligned}
& =\mathrm{n} \cdot \frac{7}{2} \mathrm{R} \Delta \mathrm{~T} \\
& =\frac{7}{9} \Delta \mathrm{Q} \\
& =7 \mathrm{~kJ}
\end{aligned}
$$

Ans. (C); I-P, II-R, III-T, IV-Q
18. List I contains four combinations of two lenses (1 and 2) whose focal lengths (in cm ) are indicated in the figures. In all cases, the object is placed 20 cm from the first lens on the left, and the distance between the two lenses is 5 cm . List II contains the positions of the final images.
(I)

Which one of the following options is correct?
(A) I $\rightarrow$ P, II $\rightarrow$ R, III $\rightarrow \mathrm{Q}, \mathrm{IV} \rightarrow \mathrm{T}$
(B) I $\rightarrow \mathrm{Q}, \mathrm{II} \rightarrow \mathrm{P}, \mathrm{III} \rightarrow \mathrm{T}, \mathrm{IV} \rightarrow \mathrm{S}$
(C) I $\rightarrow$ P, II $\rightarrow$ T, III $\rightarrow$ R, IV $\rightarrow \mathrm{Q}$
(D) I $\rightarrow$ T, II $\rightarrow$ S, III $\rightarrow$ Q, IV $\rightarrow \mathrm{R}$

Ans. (A)

## éSaral

Sol. (I) $v_{1}=\frac{u f}{u+f}$

$$
\begin{aligned}
& =\frac{(-20)(10)}{(-20)+(10)}=+20 \\
& u_{2}=+15 \\
& \mathrm{v}_{2}=\frac{(15)(15)}{(15)+(15)}=+7.5
\end{aligned}
$$

(II) $\mathrm{v}_{1}=+20$

$$
\mathrm{u}_{2}=+15
$$

$$
\mathrm{v}_{2}=\frac{(15)(-10)}{(15)+(-10)}=-30
$$

(III) $\mathrm{v}_{1}=+20$

$$
\mathrm{u}_{2}=+15
$$

$$
\mathrm{v}_{2}=\frac{(15)(-20)}{(15)+(-20)}=60
$$

(IV) $\mathrm{v}_{1}=\frac{(-20)(-20)}{(-20)+(-20)}=-10$

$$
\mathrm{u}_{2}=-15
$$

$$
\mathrm{v}_{2}=\frac{(-15)(10)}{(-15)+(10)}=30
$$

Ans. (A), I-P, II-R, III-Q, IV-T

